Quandles, racks and shelves

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A quandle is a set X with a binary operation $* : X \times X \to X$ satisfying:

- (i) For all $x \in X$, x * x = x
- (ii) For all $y \in X$, the map $\beta_y : X \to X$ defined by $\beta_y(x) = x * y$ is invertible. (iii) For all $x, y, z \in X$, (x * y) * z = (x * z) * (y * z).

The three axioms of a quandle algebraically encode the three Reidemeister moves in knot theory.

A rack is a set with a binary operation that satisfies (ii) and (iii), and a shelf is a set with a binary operation satisfying self-distributivity (iii).

In this talk, I will give an introduction to quandles, racks, shelves, and quandle rings. I will also talk about a recent joint work with Matthew Pradeep Goonewardena and Mohamed Elhamdadi on shelves.